

Quadratic equations:

$$ax^2 + bx + c = 0 \text{ has roots } \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Arithmetic series:

$$u_n = a + (n-1)d$$

$$S_n = \frac{1}{2}n(a + l) = \frac{1}{2}n[2a + (n-1)d]$$

Geometric series:

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r}$$

$$S_\infty = \frac{a}{1-r} \text{ for } |r| < 1$$

Differentiation:

function derivative

$$x^p \quad px^{p-1}$$

$$f(x) + g(x) \quad f'(x) + g'(x)$$

Integration:

function integral

$$x^p \quad \frac{1}{p+1}x^{p+1} + c, \quad p \neq -1$$

$$f'(x) + g'(x) \quad f(x) + g(x) + c$$

Trigonometry:

In the triangle ABC

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{area} = \frac{1}{2}ab \sin C$$

$$\cos^2 A + \sin^2 A \equiv 1$$

Area:

$$\text{area under a curve} = \int_a^b y \, dx$$

Laws of logarithms:

$$\log_a(xy) \equiv \log_a x + \log_a y$$

$$\log_a \left(\frac{x}{y} \right) \equiv \log_a x - \log_a y$$

$$\log_a(x^k) \equiv k \log_a x$$

Trigonometry:

$$\sec^2 A \equiv 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A \equiv 1 + \cot^2 A$$

$$\sin 2A \equiv 2 \sin A \cos A$$

$$\cos 2A \equiv \cos^2 A - \sin^2 A$$

$$\tan 2A \equiv \frac{2 \tan A}{1 - \tan^2 A}$$

Differentiation:

function	derivative
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e^x	e^x
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$\ln px \ (p > 0)$	$\frac{1}{x}$
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Integration:

function	integral
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e^x	$e^x + c$
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$\frac{1}{x}$	$\ln x + c, x \neq 0$
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Differentiation:

function derivative

$$e^{kx} \quad ke^{kx}$$

$$\sin kx \quad k \cos kx$$

$$\cos kx \quad -k \sin kx$$

$$\tan kx \quad k \sec^2 kx$$

$$f(x)g(x) \quad f'(x)g(x) + f(x)g'(x)$$

$$\frac{f(x)}{g(x)} \quad \frac{f'(x)g(x) - f(x)g'(x)}{(g(x))^2}$$

$$f(g(x)) \quad f'(g(x))g'(x)$$

Integration:

function integral

$$e^{kx} \quad \frac{1}{k} e^{kx} + c$$

$$\cos kx \quad \frac{1}{k} \sin kx + c$$

$$\sin kx \quad -\frac{1}{k} \cos kx + c$$

$$\sec^2 kx \quad \frac{1}{k} \tan kx + c$$

$$f'(g(x))g'(x) \quad f(g(x)) + c$$

Vectors:

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \cdot \begin{pmatrix} a \\ b \\ c \end{pmatrix} = xa + yb + zc$$

$$\text{Mean} = \bar{x} = \frac{\sum x}{n} \text{ or } \frac{\sum fx}{\sum f}$$

$$\text{Standard deviation} = \sqrt{\text{Variance}}$$

$$\text{Interquartile range} = \text{IQR} = Q_3 - Q_1$$

$$P(A') = 1 - P(A)$$

For independent events, $P(B | A) = P(B)$, $P(A | B) = P(A)$, $P(A \cap B) = P(A) P(B)$

$$E(aX + b) = aE(X) + b$$

$$\text{Var}(aX + b) = a^2 \text{Var}(X)$$

Cumulative distribution function for a discrete random variable:

$$F(x_0) = P(X \leq x_0) = \sum_{x \leq x_0} p(x)$$

Standardised Normal Random Variable $Z = \frac{X - \mu}{\sigma}$ where $X \sim N(\mu, \sigma^2)$

For the continuous random variable X having probability density function $f(x)$,

$$P(a < X \leq b) = \int_a^b f(x) dx.$$

$$f(x) = \frac{dF(x)}{dx},$$

$aX \pm bY \sim N(a\mu_x \pm b\mu_y, a^2\sigma_x^2 + b^2\sigma_y^2)$ where X and Y are independent and $X \sim N(\mu_x, \sigma_x^2)$ and $Y \sim N(\mu_y, \sigma_y^2)$.

The tension in an elastic string = $\frac{\lambda x}{l}$

The energy stored in an elastic string = $\frac{\lambda x^2}{2l}$

For SHM:

$$\ddot{x} = -\omega^2 x,$$

$$x = a \cos \omega t \text{ or } x = a \sin \omega t,$$

$$v^2 = \omega^2(a^2 - x^2),$$

$$T = \frac{2\pi}{\omega}$$